# **Module 2: Hydrologic Cycle**

**Concept & Average Global Water Balance**

CWR 3540: Water Resources Engineering FIU Department of Civil & Environmental Engineering Professor Fuentes

#### The Water Cycle





Figure 1.1.1a **McGraw Hill** 







Figure 1.4.1<br>Images courtesy of NASA GSFC Scientific Visualization Studio and Landsat-7 Project

# **Module 2: Hydrologic Cycle & Elements**

#### **Conservation of Mass Principle Handout:**

*(See in course website: Study Materials/Additional Handouts/Module 1)*

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# Control Volume Approach: Hydrosystems





## Drainage Basins, Watersheds, Catchments or Drainage Areas



**Figure 7.1.11** © John Wiley & Sons, Inc. All rights reserved.

# Sketch of a River Basin



Figure 7.1.1 © John Wiley & Sons, Inc. All rights reserved.

### Airport Drainage Area: Example

Figure 17.10 Section of an airport.



### Conservation of Mass Principle: Water Balance (or Budget) Equation(s)

• A general equation is Eq. 2.1:

 $P + Q_{SI} + Q_{GI} - E - Q_{SO} - Q_{GO} - \Delta s - n = 0$ , for a ΔT (1 week, 1 year, etc.) When either volumes, flow rates or mean depths for the ΔT are used

- For water bodies, short-duration (Eq. 2.2):  $P + Q_{in} - E - Q_0 - \Delta s = 0$ If inflow and outflow terms in Eq. 2.1 are combined and n is "nil"
- For large basins for Long Duration (Eq. 2.3):  $P - E - Q_0 = 0$ If surface inflow, groundwater inflow and outflow terms in Eq. 2.1 an n are ignored or "nil"
- For direct runoff in a basin, over the ground surface, during a storm Eqs. 2.4,and2.5):  $P - E - I - S_D - R = 0$  (Eq. 2.4)

If evaporation, interception and depression storage are much smaller than infiltration, Eq. 2.4 becomes:  $R = P - 1$  (Eq. 2.5)

# Discrepancy Term & Errors

Table 2.1 Percent Errors in Hydrologic Components by Commonly Used **Methodologies** 



# **Module 2: Hydrologic Cycle**

**Precipitation**

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### Forms of Precipitation

#### **TABLE 4.1 Forms of Precipitation**

and the control of the con-



 $\sim$  10  $\mu$ 

Source: Adapted from R.K. Linsley, Jr., M.A. Kohler, and J.L.H. Paulhus, Hydrology for Engi-<br>neers, 3rd ed., McGraw-Hill. Copyright © 1982 by McGraw-Hill. Used by permission.

#### Standard Rain Gage – Non-recording



**Figure 12.1.6 Courtesy of the National Oceanic and Atmospheric Agency** 

#### Weighing Bucket Rain Gage - Recording





#### Tipping Bucket Rain Gage (Exterior)



**Figure 12.1.8b** www.wikipedia.com

#### Example Rain Record and Hyetograph



ING TIME OF THE INTERVAL. DATE AND TIME ARE NOT ENTERED FOR TRACE AMOUNTS.



SOURCE: McCuen, 2.4, 3th Girlian, 2005

# Rainfall Hyetographs

• *Hyetograph:* 

*Plots of rainfall depth or intensity as function of time*

### Examples of Hyetographs:

Depth or intensity versus time Cumulative (or "rainfall mass curve")



**Figure 7.2.8** © John Wiley & Sons, Inc. All rights reserved.

#### Return Period & Probability of Exceedance of Hydrologic Events

$$
\bullet \ \mathsf{T}=1/\mathsf{P}_{\geq}
$$

### Precipitation Data Analysis (Mays, 2012) (See Example 2.6 , Gupta 2017)

Mon Feb 02 21:45:19 2009





(a) Chicago, Ilinois 41.820 N 87.67 W 593 feet

#### Precipitation Data Analysis (Mays, 2012) (See Example 2.6, Gupta 2017)



Mon Feb 02 21:45:19 2009

Average recurrence interval (years)		
10 25	$\theta$ $\overline{\phantom{a}}$	100 200 500 1000

Figure 7.2.15a part 1 © John Wiley & Sons, Inc. All rights reserved.

# Example of IDFs (Example 2.6)



Figure 2.6 Intensityduration-frequency curve.

## Example of IDFs





#### Regression Analysis: IDFs (A common, simple relationship)

Linear Regression Onalysis<br>for IDF. relation  $\vec{\mathcal{L}} = \frac{A}{\vec{\xi} + \vec{B}}$  (Eg. 2.15, Gupta, 2017) Considering Equation 2.15 (Gysta, 2017),<br>Which applies to a specific "return<br>period in years, the following is an approach:  $\frac{1}{x} = \frac{t+3}{4}$   $\frac{1}{x} = \frac{1}{A}t + \frac{8}{A}$  $\mathcal{L}^2 = \mathcal{L}$ where  $r^2$  = coefficient for index) of r = correlation

 $co$  efficient

### Intensity-Duration-Frequency Curve:  $''$ IDFs"

*Example 2.6 (i.e., development of IDFs) Equation 2.15 (e.g., empirical relationship) NWS IDF Maps: Eq. 2.15 Regional Constants*

## IDFs Constants for USA Regions

Map of similar rainfall characteristics (from Steel and McGhee, 1979). **Figure 2.7** 



### IDF General Relationships

A general equation for the IDF<br>relations is the following:  $\overline{C}$  $t^e$  +  $f$ where  $i = interest$ T = return period<br>or average recurrence interval<br>t = storm duration  $c, e, f = \frac{best - fit}{constants}$ statistical

# Solving Problems with Gages (Refer to Section 2.6)

- Two regular problems:
	- Breaks in records
	- Changes in recording conditions
- Solutions Using Neighboring Gage Sites:
	- Estimation of Missing Data
	- $-$  Eq. 2.14:  $P_x/N^x = 1/n (P_x/N_1 + P_x/N_2 + ... + P_n/N_n)$
	- Checking Data Consistency: Double Mass-Analysis:
		- Plot of accumulated values at test gage site versus accumulated values at base stations (See Figure 2.2)

#### Estimating Missing Data from Gages

(See Equation 2.14 in textbook:  $P_x/N_x = 1/n [P_1/N_1 + P_2/N_2 + ....]$ 

*("Additional example": file "1" in folder Module2<Precipitation in course website)*

As an example, consider the following data:



The storm-event catch at gage X is missing. Ten percent of the annual catch at gage X is 4.1 in., and the average annual catch at each of the three regional gages is within  $±$  4.1 in.; therefore, the station-average method can be used. The estimated catch at the gage with the missing storm-event total is

$$
\hat{P} = \frac{1}{3}(2.6 + 3.1 + 2.3) = 2.67 \text{ in.}
$$
\n(4.9)

Using this method requires knowledge of the average annual catch, even though this information is not used in computing the estimate,  $\ddot{P}$ .

# Checking Data Consistency: *Double-Mass Analysis (Example 2.3)*

Figure 2.3 Double-mass curve for Example 2.3.


Point to Areal Precipitation: Determination of Average

- Arithmetic or Station Average Method *(Example 2.4)*
- Weighted Average Methods
	- Thiessen Polygon Method *(Example 2.4)*
	- Isohyetal Method *(Example 2.5)*

## **Next Generation Radar (NEXRAD)**

#### **Radar Measurements**

#### What is it?

Reflection of electromagnetic waves from a radar antenna by raindrops

**Reflection strength =** 

f(number and size of drops)

Distance from radar site to the area  $=$ 

f(time between pulse emission and receipt of echo)

#### **Systems**

NWS installed a network of 161 Doppler radar systems in the 1990's: NEXRAD for next generation radar. WSR88D was deployed jointly by USDOE, USDOD and USDOT.

Other systems are operated by FAA, among other agencies

#### **Application**

Estimates temporal intensities over large areas

Combined with rain gage data results in estimates between areas

Less accurate than gage measurements

### NEXRAD - Example NWS



http://radar.weather.gov/Conus/southeast.php

## NEXRAD – Example NWS (Cont.)

N WS JetStream - Doppler Kedar: Base Keflectivity

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#### **Base Reflectivity**

reflectivity is excellent for surveying the region around the radar to look for precipitation. However, remember the radar beam increases in elevation as distance increases from the radar. This is due, in part, to the elevation angle itself but is more because the earth's surface curves away from the beam.

This can lead to underestimating the strength and intensity of distant storms. For this reason, it is wise to always check the radar images from different locations to help provide the overall picture of the weather in any particular area.

This image (right) is a sample base reflectivity image from the Doppler radar in Frederick, OK. The radar is located in the center of the image. The colors represent the strength of returned energy to the radar expressed in values of decibels (dBZ). The color scale is located at the lower right of each image.



Severe weather may be occurring with values less (or greater) than 60 to 65 dBZ due to...

- Hail that is totally frozen (without a thin layer of water in the surface). "Dry hail" is a very poor reflector of energy and can lead to an *underestimate* of a storm's intensity.
- Atmospheric conditions such a ducting. When ducting occurs, the radar beam is refracted into the ground (indicating stronger storms than what are actually occurring). However a worse case is

## **Module 2: Hydrologic Cycle**

**Evaporation & Transpiration**

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## Evaporation & Transpiration

("losses from runoff or groundwater)

- Evaporation: water vaporized into atmosphere from free water surface and land areas
- Transpiration: *water absorbed by plants and crops and eventually discharged into the atmosphere*
- *About 70% of the precipitation in the USA is returned to the atmosphere as either E, T or both, ET*

## Evaporation Estimates (and Measurements) from Free-Water Bodies

- Comparative methods: Pan Evaporation and Atmometers
- Aerodynamic Method
- Energy Balance Method
- Combination Method (of the aerodynamic and energy methods)

### **Standard NWS Evaporation Pans** (with Cup Anemometers)



**Figure 12.1.12a** wikimedia commons

#### **Class A Evaporation Pan**  $(E_L = KE_p)$



**Figure 12.1.12b Courtesy of the National Weather Service** 

## Evaporation Pans (from a free-water body, e.g., a lake)

- Most common method: Uses the Standard National Weather Service Class A Pan (4 ft diameter x 10 in depth, wooden frame 12 in above ground
- Equation 3.1:  $E_L = K \times E_p$ 
	- $E_1$  = evaporation from water body
	- $E_p$  = evaporation from the pan

 $K =$  pan coefficient (0.6 to 0.8 range, and average of 0.7) *Equation 3.2, Kohler and Parmele (1967) corrects K to a K' for monthly and daily evaporation* 

*losses, based on vapor pressure measurements:*

$$
E_{L} = K' \{ (e_{sl} - e_{z}) / (e_{sp} - e_{z}) \} \times E_{p}
$$

#### *Refer to Example 3.1*

# Aerodynamic Method Sketch (Source: Mays, 2012)

*It considers the transport of water vapor by the turbulence of the wind over a natural surface*





# Aerodynamic Method

- Widely used for lakes and reservoirs
- Equations: 3.3, 3.4 and 3.5, with Table 3.1
	- $-E_a = M(e_s e_z) u_z$  (LT<sup>-1</sup>), where
		- $e_a$  = evaporation by aerodynamic method
		- M =mass transfer coefficient
		- $e_s$  = saturation vapor pressure at water T
		- $e_z$  = air vapor pressure at level z  $[= RH(e_z^{\circ})]$
		- RH = relative humidity
		- $u_7$  = wind velocity at level Z
- See Example 3.2 and Additional Example in Module 2

## Reference Height for Roughness

(Used when wind speed is measured at an elevation other than that for determination (See Equation 3.5 or logarithmic law that accounts for surface roughness)



## Energy Balance Method Sketch





# Energy Method

- It is highly data intensive
- Equation 3.8, estimated as Eq. 3.9 or 3.10 plus Eq. 3.11supported by Equations 3.7, 3.8 and Table 3.1
	- $E_r = [R_n G]/[\rho_w \lambda (1 + \beta)]$  [LT<sup>-1</sup>], where
		- Where,  $R_n$  = net radiant energy (=  $S_n + R_b$ ), which are the net short-wave radiation and the net long-wave radiation, respectively
		- β, Bowen ratio, is calculated with Eq. 3.7
		- Other parameters are defined in Tables 3.2 and 3.3/ as function of temperature
- See Example 3.3

## Combined Method (of Penman)

- Weighted estimate from both the aerodynamic and energy methods
- Equation 3.13
	- $E = \Delta/[\Delta + \gamma] \times E_r + \Delta/[\Delta + \gamma] \times E_a$ , where
		- $E_r$  = evaporation by the energy method
		- $E_a$  = evaporation by the aerodynamic method
		- $\Delta$  = gradient of saturated water pressure, listed in Table 3.2 as function of temperature.
- See Example 3.4

# $C_p$ ,  $e_s$ ,  $\Delta$  of  $e_s$ ,  $\gamma$ , and  $\lambda$

#### Table 3.2 Specific Heat, Saturated Vapor Pressure, Gradient, Psychrometric Constant, and Latent Heat of Vaporization at Standard Atmospheric Pressure



## ET from a Drainage basin

- Evapotranspirometers (i.e., experimental devices also referred to as *"lysimeters", if drainage from the soil is also accounted for)*
- Penman-Monteith ET Equation (after Eq. 3.13)
	- Equation 3.16 (p. 77), which defines two "resistances", one the aerodynamic resistance from a water surface by wind as water vapor transfer into the air above,  $r_a$ , and the resistance of water vapor to move from inside the plant to the air outside,  $r_{s}$

## Evapotranspirometers

(e.g., "lysimeters")



#### Example of Field Experiment<br>
Example of System Drawing



## **Module 2: Hydrologic Cycle**

**Infiltration & Runoff**

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### Double-ring Infiltrometer



**Figure 12.1.15** www.wikipedia.com

# *Infiltration Capacity* Estimation

- Theory-based:
	- Infiltration Capacity and
	- Non-Linear Loss Rate Function
	- Green-Ampt Model (i.e., quite common)
- Empirical:
	- Horton's Equation
	- Holton's Equation & Others
- Methods for Direct Runoff that account for infiltration
	- Infiltration-Index Method
	- NRCS (or "CN") Method

## Infiltration-Rainfall Behavior



 $(a)$ 

Water content,  $\theta$ 



### Rainfall Intensity and Infiltration Rate



## Horton's Infiltration Model

- Horton (1939):
	- $-f_p = (f_o f_c) e^{-kt} + f_c$  (Eq. 4.2, p. 96), where
	- $f_0$  = initial infiltration rate
	- $f_c$  = final constant infiltration rate, equal to *"apparent "soil" saturated hydraulic conductivity"*
	- $-k$  = factor representing the rate of decrease (also referred to as *"recession constant")*
	- *See handout and example in course website*



<sup>a</sup> Successive difference col. 1

<sup>b</sup> Average of two successive values of col. 2

c col. 3 × col. 4 × 
$$
\left[\frac{1}{60} \frac{hr}{min}\right]
$$

<sup>d</sup> Cumulation of col. 5





#### Table 4.2 Revised Infiltration Capacity for the Storm of Example 4.1





Note: Computations of col. (3), (4) and (5) are similar to Table 4.1.

<sup>a</sup> Col. 
$$
6 \times \text{col. } 3 \times \left[ \frac{1}{60} \frac{\text{hr}}{\text{min}} \right]
$$

 $b$  Col. 7 – col. 5

<sup>c</sup> Negative value of the previous step.

# Infiltration Index Method to Runoff

- See types of indices, including the simplest φ-Index option and its procedure in Section 4.5.
- Applications: Examples 4.6 and 4.7

### Representation of the φ-Index



Figure 4.9 Representation of the  $\phi$  index.

## NRCS ("CN") Method for Direct Runoff

- $Q = (P 0.2S)^2 / (P + 0.8S)$  [L], where
	- $-Q$  = accumulated runoff depth over the drainage area
	- $P$  = accumulated rainfall depth
	- S = potential maximum retention of water by soil
- $CN = 1000/(10 + S)$ , where
	- CN = curve number (See Tables 4.10. 4.11, 4.12 and 4.13)
# Hydrologic Soils Types





a Reproduced from U.S. Soil Conservation Service (1986).

### Curve Numbers for AMC II



### Curve Numbers for AMC II

#### Table 4.11 Curve Numbers for Antecedent Moisture Condition II (Continued)



# Curve Numbers for AMC II

#### **Table 4.12 Antecedent Moisture Condition**



## Curve Numbers for AMC I and II As Function of AMC II

#### **Curve Number for Condition** Corresponding Curve Number for Condition  $\mathbf{H}$  $\mathbf{I}$  $\mathbf{III}$  $\overline{7}$  $\overline{4}$  $\overline{2}$  $\mathbf 0$  $\Omega$  $\Omega$

#### Table 4.13 Cross-Linking of Curve Numbers for Various Antecedent Moisture **Conditions**

Source: U.S. Soil Conservation Service (1972).

## Runoff Depth As Function of CN



<sup>a</sup> Interpolate the values shown to obtain runoff depths for CNs or rainfall amounts not shown.

Source: U.S. Soil Conservation Service (1986).

[Florida air quality check: Thank Canada fire](https://www.news-journalonline.com/story/weather/2023/10/03/canadian-wildfire-smoke-florida-air-quality-haze/71041423007/)  [smoke for hazy Florida \(news](https://www.news-journalonline.com/story/weather/2023/10/03/canadian-wildfire-smoke-florida-air-quality-haze/71041423007/)[journalonline.com\)](https://www.news-journalonline.com/story/weather/2023/10/03/canadian-wildfire-smoke-florida-air-quality-haze/71041423007/)

# **Module 2: Hydrologic Cycle**

**Streamflow**

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#### Streams, Rivers & Canals













#### Stream Channel Velocity-Distribution

Typical velocity distribution in a stream channel. **Figure 8.5** 



#### Determination of Streamflow (*or Discharge*)

• *Streamflow* quantity, space distribution and time variability are required to plan and design any surface water supply or hydraulic structure.

# Measurement & Estimation

- Measurement of Streamflow
	- Direct measurement or stream gaging
	- Through hydraulic devices (for small stream and open channels, for instance, weirs, flumes, etc.)
	- Indirect measurement of peak flows
- Estimation of Streamflow
	- Application of precipitation data
	- Extension of gage-sites data
	- Generation of synthetic flows
	- Use of generalized data, charts, tables and empirical approaches

# Stream Gaging

- Stream gaging or hydrometry measures the water stage (level or depth) and discharge at a gaging station to collect a continuous record
- A number of gaging stations in a watershed, basin or drainage area form a hydrologic network
- The US Geological Survey operates a nationwide stream-gaging network (+7,600)

## Stage-Discharge Relationship: ("Rating Curve")

Figure 8.23 Log-log plot of stage and discharge data for Example 8.11.



## Stage Measurement

- Stilling Well with Float Sensor (Fig. 8.1)
- Pressure System with Bubble-Gage Sensor (Fig. 8.2) (e.g., nitrogen)
- Radar Stage Measurement (Fig. 8.3) (e.g., sensor-emitted electromagnetic waves echoed back to the sensor)

#### Stage Measurement

Figure 8.1 Stilling well for a float-type recorder (from Herschy, 1985a).



## Bubble-gage Measurement

Figure 8.2 Bubble-gage installation (from Herschy, 1985a).



# Radar Stage Measurement

#### (Figure 8.3, Gupta, 2017)



# Single Stage-Discharge Relation

- Equation 8.25:
	- $-Q = A (h \pm a)^n$  where
		- $Q =$  discharge
		- $H =$  gage height
		- a = stage reading at zero flow (i.e., datum correction)

A, n = constants to be determined for each case

*Or*

Log  $Q = n log (h \pm a) + log A (of the form Y = M X + N)$ 

– See Sections 8.19.1 and 8.21 for regression analysis

#### Defining "a": Trial and Error Procedure

Trial-and-error procedure to determine the stage of zero flow. Figure 8.22



# Discharge Measurement

- Volumetric flow rate:  $Q = \int a \cdot dv = \sum a_i \cdot v_i$  (L T<sup>-3</sup>)
- Methods of measurement:
	- Current meter method (e.g., "Price"; mechanical meter, Fig. 8.4)
	- Hydroacoustic method (Acoustic Doppler velocity meter, ADCP, or sound pulse of certain frequency from and reflected back to transducer), with GPS to track the stream bottom (Fig. 8.16)
	- Ultrasonic method (ultrasonic velocity meter, UVM)
	- Electromagnetic method (based on electromagnetic induction, electrodes on banks and coils buried in stream section)

# Methods to Measure Velocity and Area to Determine Discharge

- Current Meter
- Hydroacoustic (e.g., acoustic Doppler velocity meter, ADVM ): sent and reflected back acoustic signal of 10 MHz frequency
- Ultrasonic (ultrasonic velocity meter, UVM)
- Electromagnetic (based on electromagnetic induction): measures electric current from water – a conductor - moving in magnetic field

#### Price Current Meter

Figure 8.4 Assembly of a type AA current meter (courtesy of Geophysical Instrument and Supply Co.).



#### Discharge Computation by Current Meter – Mid-Section Method *Example 8.7*

Subsection in the midsection method. Figure 8.9



#### Discharge Computation by Current Meter – Mean-Section Method *Example 8.8*

Figure 8.10 Subsection in the mean-section method.



Alternative Procedures to Cross the Stream or River: Using Current Meters

- By wading
- From a bridge
- From a cableway
- By boat
- Over ice cover

#### Acoustic Doppler Current Profiler, ADCP



# Links to USGS: Streamflow Measurements

• **Acoustic**

**[https://www.usgs.gov/centers/sa-](https://www.usgs.gov/centers/sa-water/science/hydroacoustic-applications-technological-advancements-streamgaging-network?qt-science_center_objects=0#qt-science_center_objects) [water/science/hydroacoustic-applications-technological-](https://www.usgs.gov/centers/sa-water/science/hydroacoustic-applications-technological-advancements-streamgaging-network?qt-science_center_objects=0#qt-science_center_objects) [advancements-streamgaging-network?qt-](https://www.usgs.gov/centers/sa-water/science/hydroacoustic-applications-technological-advancements-streamgaging-network?qt-science_center_objects=0#qt-science_center_objects) [science\\_center\\_objects=0#qt-science\\_center\\_objects](https://www.usgs.gov/centers/sa-water/science/hydroacoustic-applications-technological-advancements-streamgaging-network?qt-science_center_objects=0#qt-science_center_objects)**

#### • **General**

**[https://www.usgs.gov/special-topic/water-science-](https://www.usgs.gov/special-topic/water-science-school/science/how-streamflow-measured?qt-science_center_objects=0#qt-science_center_objects) [school/science/how-streamflow-measured?qt-](https://www.usgs.gov/special-topic/water-science-school/science/how-streamflow-measured?qt-science_center_objects=0#qt-science_center_objects) [science\\_center\\_objects=0#qt-science\\_center\\_objects](https://www.usgs.gov/special-topic/water-science-school/science/how-streamflow-measured?qt-science_center_objects=0#qt-science_center_objects)**